# Certification Report 

# Certified Reference Material 

## BAM-M112

## Pure Lead

## September 2020

| Coordinator: | Dr. Sebastian Recknagel |
| :--- | :--- |
|  | Bundesanstalt für Materialforschung und -prüfung (BAM) |
|  | Division 1.6 „Inorganic Reference Materials" |
|  | Richard-Willstätter-Str. 11 |
|  | D-12489 Berlin |
|  | Phone: +493081041111 |
|  | Fax: +4930810471111 |
|  | E-mail: sebastian.recknagel@bam.de |

## Summary

This report describes preparation, analysis and certification of the lead reference material BAM-M112. The certified reference material (CRM) is available in the form of discs (ca. 40 mm diameter and 30 mm height). It is intended for establishing and checking the calibration of optical emission spectrometry for the analysis of samples of similar matrix composition. It is also suitable for validation of wet chemical analysis methods.

The following mass fractions and uncertainties have been certified:

## Certified Values

| Element | Mass fraction ${ }^{\text {1) }}$ <br> in mg/kg | Uncertainty ${ }^{\text {2) }}$ <br> in mg/kg |
| :---: | :---: | :---: |
| Cu | 8.2 | 0.6 |
| Ni | 5.3 | 0.4 |
| Pt | 5.4 | 0.5 |
| Se | 5.2 | 0.4 |
| Te | 5.3 | 0.3 |
| 1) |  |  |
| Unweighted mean value of the means of accepted sets of data (consisting of at least 4 single results), each set <br> being obtained by a different laboratory and/or a different method of measurement. <br> Estimated expanded uncertainty U with a coverage factor of $k=2$, corresponding to a level of confidence of <br> approx. 95 \%, as defined in the Guide to the Expression of Uncertainty in Measurement, (GUM, ISO/IEC Guide <br> 98-3:2008). |  |  |

This report contains detailed information on the preparation of the CRM as well as on homogeneity investigations and on the analytical methods used for certification.
The certified values are based on the results of eight laboratories which participated in the certification inter-laboratory comparison.
Mass fractions of $\mathrm{Ag}, \mathrm{Bi}, \mathrm{S}$ and Tl are given for information.

## Content

Page
List of abbreviations ..... 5

1. Introduction. ..... 6
2. Companies/laboratories involved ..... 6
3. Candidate material ..... 7
4. Homogeneity testing ..... 7
5. Characterisation study ..... 8
5.1 Analytical methods ..... 8
5.2 Analytical results and statistical evaluation ..... 9
6. Instructions for users and stability ..... 17
7. Metrological Traceability ..... 17
8. References ..... 18
9. Information on and purchase of the CRM ..... 18
Annex 1: Calculation of uncertainty contribution of potential inhomogeneity (length) ..... 19
Annex 2: Calculation of uncertainty contribution of potential inhomogeneity (area) ..... 24

## List of abbreviations

(if not explained elsewhere)

| CRM | certified reference material |
| :--- | :--- |
| ETAAS | electrothermal atomic absorption spectrometry |
| ICP-OES | inductively coupled plasma optical emission spectrometry |
| ICP-MS | inductively coupled plasma mass spectrometry |
| SOES | spark optical emission spectrometry |
| $M$ | mean value |
| $n$ | number of accepted data sets |
| $S$ | standard deviation of an individual data set |
| $S_{\text {M }}$ | standard deviation of laboratory means |
| $S_{\text {rel }}$ | relative standard deviation |
| $\bar{S}_{i}$ | square root of mean of variances of data sets under repeatability conditions |
| $M_{i}$ | single result |
| I | ICP-OES (Tables 2-6) |
| I-D | ICP-OES after fire assay (Tables 2-6) |
| I(R) | ICP-OES, revised value (Tables 2-6) |
| IMS | ICP-MS (Tables 2 - 6) |
| IMS(R) | ICP-MS, revised value (Tables 2-6) |
| EA | ETAAS (Tables 2 - 6) |

## 1. Introduction

In the metal-producing and metal-working industry mainly spark emission spectrometry (SOES) is used for reception inspection of raw materials, e.g. scrap, for quality control of end products and production control. This time-saving analytical technique requires suitable reference materials for calibration and recalibration. The certified reference material BAM-M112 is based on pure lead and is beside other elements certified for its Pt-content. Pt becomes more and more important for lead battery production.

The idea to produce the reference material for BAM-M112 was the outcome of discussions within the working group „Lead" of the Committee of Chemists within the Society of Metallurgists und Miners (GDMB). The needs are defined by this working group, since the members are potential users of the prepared CRMs. Participating laboratories were recruited from this group. Since all these laboratories are highly experienced with lead analysis and had participated in earlier interlaboratory comparisons, there was no preceding proficiency test for qualification necessary.

Certification was carried out on the basis of ISO 17034 [1] and the relevant ISO-Guides [2, 3].

## 2. Companies/laboratories involved

## Manufacturing of the material:

- SUS Nell, Oberhausen, Germany


## Test for homogeneity:

- Aurubis AG and participating laboratories


## Participants in the certification inter-laboratory comparison:

Aurubis AG, Hamburg, Germany
Bundesanstalt für Materialforschung und -prüfung (BAM), Berlin, Germany
Berzelius Stolberg, Stolberg, Germany
Clarios Germany GmbH \& Co. KGaA, Hannover, Germany
Clarios Zwickau GmbH \& Co. KG, Zwickau, Germany
Hoppecke Batterien GmbH \& Co. KG, Brilon-Hoppecke, Germany
Muldenhütten Recycling und Umwelttechnik GmbH, Freiberg, Germany
WESER METALL GmbH, Nordenham, Germany
Statistical evaluation of the data:

- Bundesanstalt für Materialforschung und -prüfung (BAM), Berlin, Germany


## 3. Candidate material

A pure lead was used as basic material for the preparation of the candidate material. This material was milled, melted and doped with the desired impurities by SUS Nell, Oberhausen. Five sub-batches were produced ( $1-5$ ), from which cylinders were casted.
In total, 240 discs of BAM-M112 with a diameter of ca. 38 mm and 38 mm height were obtained.

## 4. Homogeneity testing

Possible reasons for an inhomogeneous distribution of elements in the raw material may be a change of the composition of the melt during the casting procedure because some elements may volatize or because of possible segregation during the solidification of the material. Since the raw material was produced by casting of a rod, concentration gradients can occur over the length of the rod (axial) as well as over the area of the rod (radial, see Figure 1):


Fig. 1: Axial and radial composition gradient

Therefore, it is necessary to investigate the raw material for both axial and radial inhomogeneities. Radial as well as axial homogeneity testing of the candidate material was done using spark emission spectrometry. In total 10 discs (two of each sub-batch) of BAM-M112 were investigated (4 sparks per disc).

The estimate of analyte-specific inhomogeneity contribution $u_{b b}$ to be included into the total uncertainty budget was calculated according to ISO Guide 35 [4] using Eq. (1) and Eq. (2):

$$
\begin{align*}
& s_{\mathrm{bb}}=\sqrt{\frac{M S_{\mathrm{among}}-M S_{\text {within }}}{n}}  \tag{1}\\
& u_{\mathrm{bb}}^{*}=\sqrt{\frac{M S_{\text {within }}}{n}} \sqrt[4]{\frac{2}{N(n-1)}} \tag{2}
\end{align*}
$$

where:

| $M S_{\text {among }}$ | mean of squared deviations between discs (from 1-way ANOVA, see |
| :--- | :--- |
|  | Annex 1) |
| $M S_{\text {within }}$ | mean of squared deviations within one disc (from 1-way ANOVA) |
| $n$ | number of replicate measurements per disc |
| $N$ | number of discs selected for homogeneity study |

$s_{\mathrm{bb}}$ signifies the between-discs standard deviation whereas $u_{\mathrm{bb}}^{*}$ denotes the maximum heterogeneity that can potentially be hidden by an insufficient repeatability of the applied measurement method (which has to be considered as the minimum uncertainty contribution). In any case the larger of the two values was used as $u_{\text {bo }}$ (1) for inhomogenity over the length. Eq. (1) does not apply if $M S_{\text {within }}$ is larger than $M S_{\text {among. }}$.
In addition to the tests performed over the length of the rods nine laboratories participated in a spark OES round robin. They were asked to perform the analysis following the given routine: outer circle: 4 sparks, inner circle: 4 sparks; centre: 1 spark. From this investigation no hint to any inhomogeneity over the area was obtained. The uncertainty contribution was calculated with the data obtained from two of the laboratories (Aurubis AG (Lab. A), Clarios Hannover (Lab. B)).
The analyte-specific within-disc uncertainty component $u_{b c}(2)$ was calculated in the same way as for the total batch. To calculate the necessary data an unbalanced ANOVA was carried out considering that the number of single measurements is different for the centre, the inner and the outer circle. For technical reasons, at r_0 (centre) only one measurement is possible. An ANOVA requires a minimum of two measurements per factor value. Thus, the value for r_0 should be replaced by a dummy. This dummy is defined as follows:
The two values replacing the measured one have a mean equal to the value measured, and a standard deviation equal to the average within-variation. This resembles the situation where one could take two independent measurements at the same place, with values deviating by the average standard deviation (non-destructive testing method). A measure for the average standard deviation is calculated from the data for r_in (inner circle) and r_out (outer circle). The result from these calculations is an inhomogeneity component for the radius of the disc. From these values, a combined inhomogeneity component is calculated. This component is compared with the within standard deviation calculated from the ANOVA-data. The higher component (square root of the mean of variances from the two labs) is used for the uncertainty calculation.
The results of the calculations are given in the annex.

## 5. Characterisation study

### 5.1 Analytical methods

Nine laboratories participated in the certification inter-laboratory comparison. For some elements part of the laboratories used more than one analytical method reporting more than one data set.
The laboratories were asked to analyse six subsamples. They were free to choose any suitable analytical method. Table 1 shows the analytical methods used by the participating laboratories.
For all analytical methods where a calibration was necessary this calibration was performed using liquid standard solutions. All participating laboratories were asked to use only standard solutions prepared from pure metals or stoichiometric compounds or well checked commercial calibration solutions.

Table 1: Analytical procedures used by the participating laboratories

| Lab-No. | Element | Sample mass | Sample pretreatment | Analytical method |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\begin{aligned} & \hline \mathrm{Cu}, \mathrm{Ni}, \mathrm{Pt}, \mathrm{Se}, \\ & \mathrm{Te} \end{aligned}$ | 2 g | Dissolution $\mathrm{HNO}_{3} / \mathrm{HCl}$ | ICP-OES with matrix matched standards (Pb 99.9995\%), calibration with commercial solutions (Spex certified) |
|  | Pt | 5 g | Melting with 10 mg Ag to collect Pt, separation of lead, dissolution of Ag in $\mathrm{HNO}_{3} / \mathrm{HCl}$ | ICP-OES, calibration with commercial solutions (Spex certified) |
| 2 | $\mathrm{Cu}, \mathrm{Ni}, \mathrm{Se}, \mathrm{Te}$ | 0.5 g | Dissolution $\mathrm{HNO}_{3}$ | ICP-MS, calibration with commercial solutions (Merck certipur) |
|  | Pt | 2 g | Dissolution with $\mathrm{HNO}_{3}$ and HCl at $200^{\circ} \mathrm{C}$ | ICP-OES with matrix matched standards (Pb 99.999\%), calibration with commercial solutions (Merck certipur) |
|  | Pt | 0.5 g | Dissolution with $\mathrm{HNO}_{3}$ and HCl at $200^{\circ} \mathrm{C}$ | ICP-MS, calibration with commercial solutions (Merck certipur) |
| 3 | $\mathrm{Cu}, \mathrm{Ni}, \mathrm{Se}, \mathrm{Te}$ | 2 g | Dissolution with tartaric acid/ $\mathrm{HNO}_{3}$ (acc. prEN 13800) | ICP-OES, with matrix matched standards, calibration with commercial solutions (Merck, NIST traceable) |
|  | Pt | 5 g | Melting with 10 mg Ag to collect Pt, separation of lead, dissolution of Ag in $\mathrm{HNO}_{3} / \mathrm{HCl}$ | ICP-OES, calibration with commercial solutions (Merck, NIST traceable) |
| 4 | $\mathrm{Cu}, \mathrm{Ni}, \mathrm{Se}, \mathrm{Te}$ | 2 g | Dissolution with tartaric acid/ $/ \mathrm{HNO}_{3}$ (acc. prEN 13800) precipitation of Pb as sulfate | ICP-OES, calibration with commercial solutions (Merck certipur) |
|  | Pt | 2 g | Dissolution with aqua regia, precipitation of Pb as sulfate | ICP-OES, calibration with commercial solutions (Merck certipur) |
| 5 | $\begin{aligned} & \hline \mathrm{Cu}, \mathrm{Ni}, \mathrm{Pt}, \mathrm{Se}, \\ & \mathrm{Te} \end{aligned}$ | 2 g | Dissolution with tartaric acid/ $\mathrm{HNO}_{3}$ (acc. prEN 13800) | ICP-OES with matrix matched standards, commercial mono-element solutions (Merck) |
| 6 | $\begin{aligned} & \hline \mathrm{Cu}, \mathrm{Ni}, \mathrm{Pt}, \mathrm{Se}, \\ & \mathrm{Te} \end{aligned}$ | 2 g | Dissolution with tartaric acid/ $/ \mathrm{HNO}_{3}$ | ICP-OES with matrix matched standards, calibration with commercial solutions (Kraft) |
| 7 | $\mathrm{Cu}, \mathrm{Ni}, \mathrm{Se}, \mathrm{Te}$, Ag, Bi, TI | 2 g | Dissolution with tartaric acid/ $\mathrm{HNO}_{3}$ | ICP-OES with matrix matched standards, calibration with commercial solutions (Merck, Kraft) |
| 9 | Cu | 0.25 g | Dissolution with $\mathrm{HNO}_{3}$ | ETAAS with commercial mono-element solution (Merck certipur) |
|  | Ni | 0.1 g | Dissolution with $\mathrm{HNO}_{3}$ | ETAAS with commercial mono-element solution (Merck certipur) |

### 5.2 Analytical results and statistical evaluation

The analytical results of the certification inter-laboratory comparison are listed in Tables 2 to 6. These tables show the single results ( $M_{i}$ ) of each laboratory, the respective laboratories' mean values ( $M$ ), absolute and relative intra-laboratory standard deviation (s and $S_{\text {rel }}$, respectively), the standard deviation of laboratory means $\left(s_{M}\right)$, and in addition the square root of mean of variances of data sets under repeatability conditions ( $\bar{s}_{\mathrm{i}}$ ) where $n$ is the number of accepted data sets. The continuous line marks the certified value (mean of the laboratories' means), the broken lines mark the standard deviation, calculated from the laboratories' means.
In the related figures for each laboratory its mean value and single standard deviation is given. Outliers which have been excluded are highlighted in yellow. This was the case for two values for Pt where the laboratories had problems to completely dissolve the platinum.

Table 2: Results for Cu in BAM-M112


Table 3: Results for Ni in BAM-M112

| Lab./Meth. | 1/I | 2/IMS | 7/I | 6/I | 4/I | 3/1 | 5/I | 9/EA |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $M_{i}[\mathrm{mg} / \mathrm{kg}]$ | 5.0 | 5.2 | 5.2 | 5.3 | 5.3 | 5.4 | 5.4 | 5.6 |  | $n$8 |
|  | 5.0 | 5.2 | 5.3 | 5.3 | 5.4 | 5.3 | 5.4 | 6.6 |  |  |
|  | 5.1 | 5.2 | 5.2 | 5.3 | 5.2 | 5.3 | 5.5 | 5.4 |  |  |
|  | 5.1 | 5.2 | 5.2 | 5.3 | 5.4 | 5.3 | 5.4 | 5.2 |  |  |
|  | 5.1 | 5.2 | 5.2 | 5.3 | 5.3 | 5.3 | 5.5 | 5.5 |  |  |
|  | 5.1 | 5.2 | 5.2 | 5.2 | 5.2 | 5.4 | 5.5 | 6.1 |  |  |
| $M$ [mg/kg] | 5.06 | 5.21 | 5.22 | 5.28 | 5.30 | 5.33 | 5.46 | 5.74 |  | 5.33 |
| $s$ [mg/kg] | 0.027 | 0.027 | 0.041 | 0.041 | 0.087 | 0.052 | 0.043 | 0.512 | $\mathrm{s}_{\mathrm{M}}[\mathrm{mg} / \mathrm{kg}]$ | 0.205 |
|  |  |  |  |  |  |  |  |  | $\bar{s}_{i}[\mathrm{mg} / \mathrm{kg}]$ | 0.187 |
| $\mathrm{S}_{\text {rel }}$ | 0.005 | 0.005 | 0.008 | 0.008 | 0.016 | 0.010 | 0.008 | 0.089 |  | 0.038 |



Table 4: Results for Pt in BAM-M112

| Lab./Meth. | $6 / \mathrm{I}$ | $5 / \mathrm{I}$ | $4 / \mathrm{I}(\mathrm{R})$ | $3 / \mathrm{I}-\mathrm{D}$ | $2 / \mathrm{IMS}(\mathrm{R})$ | $1 / \mathrm{I}-\mathrm{D}$ | $2 / \mathrm{I}$ | $1 / \mathrm{I}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $M_{\mathrm{i}}[\mathrm{mg} / \mathrm{kg}]$ | 1.6 | 2.6 | 4.8 | 5.4 | 5.5 | 5.4 | 5.1 | 5.8 |  | $n$ |
|  | 1.7 | 2.3 | 4.5 | 5.4 | 5.5 | 5.6 | 6.1 | 5.8 |  | 6 |
|  | 1.5 | 2.6 | 4.6 | 5.3 | 5.5 | 5.6 | 5.3 | 6.0 |  |  |
|  | 2.2 | 3.0 | 4.3 | 5.3 | 5.5 | 5.6 | 6.3 | 6.0 |  |  |
|  | 1.6 | 2.7 | 4.2 | 5.4 | 5.5 |  | 5.8 | 5.8 |  |  |
|  | 1.5 | 2.6 | 4.3 | 5.3 | 5.5 |  | 5.7 | 5.8 |  |  |
|  |  |  |  |  |  |  |  |  |  |  |
| $M$ [mg/kg] | 1.68 | 2.64 | 4.46 | 5.35 | 5.49 | 5.55 | 5.71 | 5.85 |  | 5.40 |
| $s[\mathrm{mg} / \mathrm{kg}]$ | 0.264 | 0.240 | 0.218 | 0.055 | 0.019 | 0.100 | 0.459 | 0.087 | $\mathrm{~s}_{\mathrm{M}}[\mathrm{mg} / \mathrm{kg}]$ | 0.496 |
|  |  |  |  |  |  |  |  |  | $\bar{s}_{\mathrm{i}}[\mathrm{mg} / \mathrm{kg}]$ | 0.216 |
| $\mathrm{~S}_{\text {rel }}$ | 0.157 | 0.091 | 0.049 | 0.010 | 0.004 | 0.018 | 0.080 | 0.015 |  | 0.092 |



Table 5: Results for Se in BAM-M112

| Lab./Meth. | 6/1 | 4/1 | 2/IMS | 1/I | 7/1 | 3/1 | 5/I |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $M_{i}[\mathrm{mg} / \mathrm{kg}]$ | 4.8 | 5.2 | 5.3 | 5.2 | 5.4 | 5.3 | 5.6 |  | $n$7 |
|  | 4.9 | 5.0 | 5.1 | 5.1 | 5.3 | 5.4 | 5.2 |  |  |
|  | 4.4 | 5.1 | 5.2 | 5.3 | 5.4 | 5.5 | 5.6 |  |  |
|  | 4.7 | 4.8 | 5.3 | 5.4 | 5.5 | 5.3 | 5.7 |  |  |
|  | 4.8 | 4.7 | 5.2 | 5.3 | 5.6 | 5.9 | 5.6 |  |  |
|  | 4.7 | 5.1 | 5.2 | 5.2 | 5.6 | 5.5 | 5.6 |  |  |
| M [mg/kg] | 4.72 | 4.98 | 5.22 | 5.23 | 5.47 | 5.48 | 5.52 |  | 5.23 |
| $s$ [mg/kg] | 0.172 | 0.191 | 0.067 | 0.109 | 0.121 | 0.223 | 0.168 | $s_{M}[\mathrm{mg} / \mathrm{kg}]$ | 0.297 |
|  |  |  |  |  |  |  |  | $\bar{s}_{i}[\mathrm{mg} / \mathrm{kg}]$ | 0.158 |
| $\mathrm{S}_{\text {rel }}$ | 0.037 | 0.038 | 0.013 | 0.021 | 0.022 | 0.041 | 0.030 |  | 0.057 |



Table 6: Results for Te in BAM-M112

| Lab./Meth. | 7/1 | 2/IMS | 3/1 | 5/I | 6/1 | 4/1 | 1/I |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $M_{i}[\mathrm{mg} / \mathrm{kg}]$ | 4.9 | 5.1 | 5.8 | 5.21 | 5.3 | 5.6 | 5.6 |  | $n$7 |
|  | 5.1 | 5.1 | 5.1 | 5.34 | 5.3 | 5.6 | 5.6 |  |  |
|  | 5.0 | 5.1 | 4.9 | 5.17 | 5.3 | 5.3 | 5.5 |  |  |
|  | 4.9 | 5.3 | 4.8 | 5.21 | 5.3 | 5.9 | 5.7 |  |  |
|  | 4.7 | 5.2 | 5.3 | 5.30 | 5.3 | 5.4 | 5.7 |  |  |
|  | 4.6 | 5.3 | 5.3 | 5.27 | 5.2 | 5.1 | 5.6 |  |  |
| $M$ [mg/kg] | 4.87 | 5.18 | 5.20 | 5.25 | 5.28 | 5.48 | 5.61 |  | 5.27 |
| $s$ [mg/kg] | 0.186 | 0.092 | 0.358 | 0.064 | 0.041 | 0.257 | 0.063 | $s_{M}[\mathrm{mg} / \mathrm{kg}]$ | 0.237 |
|  |  |  |  |  |  |  |  | $\bar{s}_{i}[\mathrm{mg} / \mathrm{kg}]$ | 0.188 |
| $\mathrm{S}_{\text {rel }}$ | 0.038 | 0.018 | 0.069 | 0.012 | 0.008 | 0.047 | 0.011 |  | 0.045 |



One laboratory determined the elements $\mathrm{Ag}, \mathrm{Bi}$ and TI with ICP-OES as well. These elements are given for information.
The data was statistically evaluated to detect outlying values (Grubbs, Nalimov, Dixon, Cochran). The Cochran-test was performed only once. The following results were obtained:

Tab. 7: Outcome of statistical tests on the results obtained for Cu and Ni

|  | Cu | Ni |
| :--- | :--- | :--- |
| Number of data sets | 8 | 8 |
| Scheffe's test (data compatible?) | yes | yes |
| Snedecor-F-Test and Bartlett-Test | Pooling not allowed | Pooling not allowed |
| Dixon $(\mathbf{\alpha}=0.05)$ | --- | --- |
| Dixon $(\alpha=0.01)$ | --- | --- |
| Nalimov $(\alpha=0.05)$ | --- | Lab. 9 |
| Nalimov $(\alpha=0.01)$ | --- | --- |
| Grubbs $(\alpha=0.05)$ | --- | Lab. 9 |
| Grubbs $(\alpha=0.01)$ | --- | --- |
| Grubbs Pair $(\alpha=0.05)$ | --- | --- |
| Grubbs Pair $(\alpha=0.01)$ | --- | --- |
| Cochran ( $\alpha=0.01)$ | Lab. 9 | Lab. 9 |
| Kolmogorov-Smirnov-Lilliefors Test | Distribution: normal | Distribution: normal |

The outliers were not removed.

Table 8: Outcome of statistical tests of results obtained for Pt in BAM-M112

|  | $1^{\text {st run }}$ | $2^{\text {nd }}$ run |
| :--- | :--- | :--- |
| Number of data sets | 8 | 6 |
| Scheffe's test (data compatible?) | yes | yes |
| Snedecor-F-Test and Bartlett-Test | Pooling not allowed | Pooling not allowed |
| Dixon $(\mathbf{\alpha}=0.05)$ | --- | Lab. 4 |
| Dixon $(\mathbf{\alpha}=0.01)$ | --- | --- |
| Nalimov $(\mathbf{\alpha}=0.05)$ | --- | Lab. 4 |
| Nalimov $(\alpha=0.01)$ | --- | --- |
| Crubbs $(\mathbf{\alpha}=0.05)$ | --- | Lab. 4 |
| Crubbs $(\mathbf{\alpha}=0.01)$ | --- | --- |
| Crubbs Pair $(\alpha=0.05)$ | Labs. 6 and 5 | --- |
| Crubbs Pair $(\alpha=0.01)$ | Labs. 6 and 5 | --- |
| Cochran $(\mathbf{\alpha}=0.01)$ | Lab. 2 | Lab. 2 |
| Kolmogorov-Smirnov-Lilliefors Test | Distribution: normal | Distribution: normal |

The Grubbs-outliers (Labs. 6 and 5, $1^{\text {st }}$ run) were removed, the outlier (Lab. 4, $2^{\text {nd }}$ run) was not removed.

Tab. 9: Outcome of statistical tests on the results obtained for Se and Te

|  | Se | Te |
| :--- | :--- | :--- |
| Number of data sets | 7 | 7 |
| Scheffe's test (data compatible?) | yes | yes |
| Snedecor-F-Test and Bartlett-Test | Pooling not allowed | Pooling not allowed |
| Dixon $(\alpha=0.05)$ | --- | --- |
| Dixon $(\alpha=0.01)$ | --- | --- |
| Nalimov $(\alpha=0.05)$ | Lab. 6 | --- |
| Nalimov $(\alpha=0.01)$ | --- | --- |
| Grubbs $(\alpha=0.05)$ | --- | --- |
| Grubbs $(\alpha=0.01)$ | --- | --- |
| Grubbs Pair $(\alpha=0.05)$ | --- | --- |
| Grubbs Pair $(\alpha=0.01)$ | --- | --- |
| Cochran $(\alpha=0.01)$ | --- | Lab. 3 |
| Kolmogorov-Smirnov-Lilliefors Test | Distribution: normal | Distribution: normal |

The outliers were not removed.

The certified mass fractions of all elements were calculated as mean of the accepted data sets. These values are given in Table 10.
The respective combined uncertainties ( $u_{\text {comb }}$ ) were calculated from the spread resulting from the certification inter-laboratory comparison ( $u_{i i c}$ ) and the uncertainty contributions from possible inhomogeneity over the length $\left(u_{\mathrm{bo}}(1)\right)$ and over area ( $u_{\mathrm{bb}}(2)$ ) of the material using Equation 3.
$u_{c o m b}=\sqrt{u_{i l c}^{2}+u_{b b}^{2}(1)+u_{b b}^{2}(2)}$
with
$u_{\text {ic }}=\sqrt{\frac{S_{\mathrm{M}}^{2}}{n}}$ : uncertainty contribution resulting from inter-laboratory comparison
$n$ : number of data sets used for calculating the certified mass fraction of each element

Table 10: Uncertainty calculation for BAM-M112

|  |  | uncertainty contribution from |  |  |  |  |  |  | $u_{b b}$ (rel) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | M | n | $5_{M}$ | $\mathrm{u}_{\text {ilc }}$ | $\begin{aligned} & u_{b b}(1) \\ & \text { Length } \end{aligned}$ | $u_{b b} \text { (2) }$ <br> Area | $u$ (comb) | $U$ | Length | Area* |
|  | $\mathrm{mg} / \mathrm{kg}$ |  | $\mathrm{mg} / \mathrm{kg}$ | $\mathrm{mg} / \mathrm{kg}$ | mg/kg | mg/kg | mg/kg | mg/kg |  |  |
| Cu | 8.18 | 8 | 0.30 | 0.1072 | 0.2341 | 0.1003 | 0.2763 | 0.5527 | 2.8619 | 1.2267 |
| Ni | 5.33 | 8 | 0.20 | 0.0724 | 0.1160 | 0.0629 | 0.1505 | 0.3010 | 2.1760 | 1.1804 |
| Pt | 5.40 | 6 | 0.50 | 0.2024 | 0.0365 | 0.1124 | 0.2343 | 0.4687 | 0.6751 | 2.0816 |
| Se | 5.23 | 7 | 0.30 | 0.1123 | 0.1272 | 0.0780 | 0.1868 | 0.3735 | 2.4314 | 1.4916 |
| Te | 5.27 | 7 | 0.24 | 0.0897 | 0.0907 | 0.0641 | 0.1428 | 0.2856 | 1.7218 | 1.2166 |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | mean of L | $A$ and B |

The expanded uncertainties $U$ are calculated by multiplication of $u_{\text {comb }}$ with a coverage factor of $k=2$ using Equation 4.
$U=k \cdot u_{\text {comb }}$
The calculated mass fractions and their resp. expanded uncertainties are given on Page 3 of this report. Rounding was done according to DIN 1333 [4].
In addition to the wet chemical characterization some of the laboratories analysed the material with spark emission spectrometry to check if there is agreement between SOES and wet chemistry. Tab. 11 shows the mean values of wet chemical and spark emission results as well as their standard deviations. The agreement between wet chemistry and SOES is given for all elements.

Tab. 11: Comparison wet chemistry vs. SOES (BAM-M112)

| Element | Wet chemical analysis |  |  | Spark emission |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mass fraction <br> in \% | Std.-dev. <br> in $\%$ | $\boldsymbol{n}$ | Mass fraction <br> in $\%$ | Std.-dev. <br> in $\%$ | $\boldsymbol{n}$ |
| Cu | 8.2 | 0.3 | 8 | 8.8 | 1.8 | 13 |
| Ni | 5.33 | 0.21 | 8 | 5.6 | 0.5 | 11 |
| Pt | 5.4 | 0.5 | 6 | 5.44 | 0.24 | 7 |
| Se | 5.23 | 0.30 | 7 | 4.8 | 1.4 | 11 |
| Te | 5.27 | 0.24 | 7 | 5.5 | 2.1 | 13 |

Three laboratories determined the elements $\mathrm{Ag}, \mathrm{Bi}, \mathrm{S}$ and TI with SOES as well. These elements are given for information.

## 6. Instructions for users and stability

The certified reference material BAM-M112 is intended for the calibration and quality control of spark emission spectrometers used for the analysis of materials with similar matrix composition. It is also suitable for validation of wet chemical analysis methods.
The surface of the material should be cleaned by turning or milling before analysis.
If chips prepared from the compact material are used for wet chemical analysis, a minimum sample intake of 0.1 g has to be used.
The material will remain stable provided that it is not subjected to excessive heat (e.g, during preparation of the working surface).

## 7. Metrological Traceability

To ensure traceability of the certified mass fractions to the SI (Système International d'Unités) calibration was performed using standard solutions prepared from pure metals or stoichiometric compounds or well checked commercial calibration solutions.

## 8. References

[1] DIN EN ISO 17034, General requirements for the competence of reference material producers, 2016
[2] ISO Guide 31, Reference materials - Contents of certificates, labels and accompanying documentation, 2015
[3] ISO Guide 35, Reference materials - Guidance for characterization and assessment of homogeneity and stability, 2017
[4] DIN 1333:1992-02 Zahlenangaben

## 9. Information on and purchase of the CRM

Certified reference materials BAM-M112 are supplied by

## Bundesanstalt für Materialforschung und -prüfung (BAM)

Division 1.6 „Inorganic Reference Materials"
Richard-Willstätter-Str. 11, D-12489 Berlin, Germany
Phone +49 30-81042061
Fax: $\quad+4930-810472061$
E-mail: sales.crm@bam.de
Each disc of BAM-M112 will be distributed together with a detailed certificate containing the certified values and their uncertainties, the mean values and standard deviations of all accepted data sets and information on the analytical methods used and the names of the participating laboratories. Information on certified reference materials can be obtained from BAM, https://www.bam.de.
Tel. +49 3081041111.

Annex 1: Calculation of uncertainty contribution of potential inhomogeneity (length) Copper in BAM-M112:

| 1A | 9.13 | 9.52 | 9.15 | 9.5 |
| :--- | ---: | ---: | ---: | ---: |
| 1E | 9.27 | 9.48 | 9.37 | 9.48 |
| 2A | 9.07 | 9.42 | 9.29 | 9.53 |
| 2E | 9.39 | 9.4 | 9.1 | 9.41 |
| 3A | 8.84 | 9.31 | 8.8 | 9.1 |
| 3E | 8.88 | 8.96 | 8.45 | 9.01 |
| 4A | 8.88 | 8.72 | 8.39 | 8.95 |
| 4E | 8.79 | 8.63 | 8.37 | 8.86 |
| 5A | 8.83 | 8.95 | 8.64 | 8.98 |
| 5E | 8.98 | 9.16 | 8.46 | 9.07 |


| Sample | Number | Sum | Mean | Variance |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample 1A | 4 | 37.3 | 9.325 | 0.04576667 |  |  |
| Sample 1B | 4 | 37.6 | 9.4 | 0.0102 |  |  |
| Sample 2A | 4 | 37.31 | 9.3275 | 0.03909167 |  |  |
| Sample 2B | 4 | 37.3 | 9.325 | 0.02256667 |  |  |
| Sample 3A | 4 | 36.05 | 9.0125 | 0.057025 |  |  |
| Sample 3B | 4 | 35.3 | 8.825 | 0.06536667 |  |  |
| Sample 4A | 4 | 34.94 | 8.735 | 0.06216667 |  |  |
| Sample 4B | 4 | 34.65 | 8.6625 | 0.04729167 |  |  |
| Sample 5A | 4 | 35.4 | 8.85 | 0.0238 |  |  |
| Sample 5B | 4 | 35.67 | 8.9175 | 0.098425 |  |  |
|  |  |  | 9.038 |  |  |  |
|  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical Fvalue |
| Between groups | 2.83314 | 9 | 0.314793333 | 6.67359197 | $3.4032 \mathrm{E}-05$ | 2.21069698 |
| Within groups | 1.4151 | 30 | 0.04717 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 4.24824 | 39 |  |  |  |  |
|  |  |  |  |  |  |  |
| within-sd | 0.217186556 |  |  |  |  |  |
|  |  |  |  |  |  |  |
| effective n | 4.00 |  |  |  |  |  |
| s_bb | 0.258661619 |  |  |  |  |  |
| s_bb_min | 0.055179801 |  |  |  |  |  |
| u_bb | 0.258661619 | 258.661619 |  |  |  |  |
|  |  |  |  |  |  |  |
| u_bb (rel.) | 2.86193427 |  |  |  |  |  |

Nickel in BAM-M112:

| 1A | 6.48 | 6.45 | 6.54 | 6.3 |
| :--- | ---: | ---: | ---: | ---: |
| 1E | 6.51 | 6.38 | 6.51 | 6.33 |
| 2A | 6.51 | 6.4 | 6.45 | 6.35 |
| 2E | 6.2 | 6.31 | 6.61 | 6.34 |
| 3A | 6.47 | 6.18 | 6.44 | 6.29 |
| 3E | 6.38 | 6.16 | 6.36 | 6.18 |
| $4 A$ | 6.05 | 6.11 | 6.32 | 6.1 |
| $4 E$ | 5.96 | 6.09 | 6.26 | 6.14 |
| 5A | 6.17 | 5.98 | 6.34 | 6.11 |
| 5E | 5.96 | 6.08 | 6.2 | 5.93 |


| Sample | Number | Sum | Mean | Variance |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample 1A | 4 | 25.77 | 6.4425 | 0.010425 |  |  |
| Sample 1B | 4 | 25.73 | 6.4325 | 0.008425 |  |  |
| Sample 2A | 4 | 25.71 | 6.4275 | 0.00469167 |  |  |
| Sample 2B | 4 | 25.46 | 6.365 | 0.0303 |  |  |
| Sample 3A | 4 | 25.38 | 6.345 | 0.0183 |  |  |
| Sample 3B | 4 | 25.08 | 6.27 | 0.01346667 |  |  |
| Sample 4A | 4 | 24.58 | 6.145 | 0.0143 |  |  |
| Sample 4B | 4 | 24.45 | 6.1125 | 0.015425 |  |  |
| Sample 5A | 4 | 24.6 | 6.15 | 0.02233333 |  |  |
| Sample 5B | 4 | 24.17 | 6.0425 | 0.015225 |  |  |
|  |  |  | 6.27325 |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F- <br> value |
| Between groups | 0.8084025 | 9 | 0.0898225 | 5.87491143 | 0.00010307 | 2.21069698 |
| Within groups | 0.458675 | 30 | 0.015289167 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 1.2670775 | 39 |  |  |  |  |



Platinum in BAM-M112:

| 1A | 6.72 | 6.85 | 6.69 | 6.59 |
| :---: | :---: | :---: | :---: | :---: |
| 1E | 6.98 | 6.7 | 6.86 | 6.48 |
| 2A | 6.91 | 6.82 | 6.73 | 6.43 |
| 2E | 6.63 | 6.57 | 6.83 | 6.74 |
| 3A | 7.06 | 6.58 | 6.73 | 6.69 |
| 3E | 6.53 | 6.55 | 6.95 | 6.61 |
| 4A | 6.58 | 6.46 | 6.77 | 6.55 |
| 4 E | 6.41 | 6.37 | 6.9 | 6.56 |
| 5A | 6.6 | 6.59 | 6.79 | 6.51 |
| 5E | 6.6 | 6.5 | 6.83 | 6.45 |


| Sample | Number | Sum | Mean | Variance |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample 1A | 4 | 26.85 | 6.7125 | 0.01149167 |  |  |
| Sample 1B | 4 | 27.02 | 6.755 | 0.04676667 |  |  |
| Sample 2A | 4 | 26.89 | 6.7225 | 0.043425 |  |  |
| Sample 2B | 4 | 26.77 | 6.6925 | 0.01335833 |  |  |
| Sample 3A | 4 | 27.06 | 6.765 | 0.0427 |  |  |
| Sample 3B | 4 | 26.64 | 6.66 | 0.03853333 |  |  |
| Sample 4A | 4 | 26.36 | 6.59 | 0.017 |  |  |
| Sample 4B | 4 | 26.24 | 6.56 | 0.05806667 |  |  |
| Sample 5A | 4 | 26.49 | 6.6225 | 0.01409167 |  |  |
| Sample 5B | 4 | 26.38 | 6.595 | 0.02843333 |  |  |
|  |  |  | 6.6675 |  |  |  |
|  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares <br> (MS) | F-value | P-value | critical Fvalue |
| Between groups | 0.19095 | 9 | 0.021216667 | 0.67597706 | 0.72400949 | 2.21069698 |
| Within groups | 0.9416 | 30 | 0.031386667 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 1.13255 | 39 |  |  |  |  |
|  |  |  |  |  |  |  |
| within-sd | 0.177162825 |  |  |  |  |  |
|  |  |  |  |  |  |  |
| effective n | 4.00 |  |  |  |  |  |
| s_bb | 0 |  |  |  |  |  |
| s_bb_min | 0.045011117 |  |  |  |  |  |
| u_bb | 0.045011117 | 45.0111166 |  |  |  |  |
|  |  |  |  |  |  |  |
| u_bb (rel.) | 0.675082364 |  |  |  |  |  |

Selenium in BAM-M112:

| 1 A | 4.65 | 4.73 | 4.83 | 4.78 |
| :--- | ---: | ---: | ---: | ---: |
| 1 E | 4.82 | 4.79 | 4.81 | 4.93 |
| 2 A | 4.67 | 5.03 | 4.78 | 4.89 |
| 2 E | 4.77 | 4.87 | 4.63 | 4.83 |
| 3 A | 4.8 | 4.68 | 4.7 | 4.8 |
| 3E | 4.7 | 4.5 | 4.57 | 4.59 |
| 4 A | 4.8 | 4.7 | 4.51 | 4.8 |
| 4 E | 4.52 | 4.57 | 4.66 | 4.81 |
| 5 A | 4.69 | 4.64 | 4.8 | 4.67 |
| 5 E | 4.52 | 4.4 | 4.45 | 4.33 |


| Sample | Number | Sum | Mean | Variance |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample 1A | 4 | 18.99 | 4.7475 | 0.00589167 |  |  |
| Sample 1B | 4 | 19.35 | 4.8375 | 0.00395833 |  |  |
| Sample 2A | 4 | 19.37 | 4.8425 | 0.02369167 |  |  |
| Sample 2B | 4 | 19.1 | 4.775 | 0.01103333 |  |  |
| Sample 3A | 4 | 18.98 | 4.745 | 0.0041 |  |  |
| Sample 3B | 4 | 18.36 | 4.59 | 0.00686667 |  |  |
| Sample 4A | 4 | 18.81 | 4.7025 | 0.01869167 |  |  |
| Sample 4B | 4 | 18.56 | 4.64 | 0.0162 |  |  |
| Sample 5A | 4 | 18.8 | 4.7 | 0.00486667 |  |  |
| Sample 5B | 4 | 17.7 | 4.425 | 0.00643333 |  |  |
|  |  |  | 4.7005 |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical Fvalue |
| Between groups | 0.56179 | 9 | 0.062421111 | 6.13575797 | 7.1177E-05 | 2.21069698 |
| Within groups | 0.3052 | 30 | 0.010173333 |  |  |  |
| Total | 0.86699 | 39 |  |  |  |  |
| within-sd | 0.100862943 |  |  |  |  |  |
| effective n | 4.00 |  |  |  |  |  |
| s_bb | 0.114288864 |  |  |  |  |  |
| s_bb_min | 0.025625882 |  |  |  |  |  |
| u_b.b | 0.114288864 | 114.288864 |  |  |  |  |
| u_bb (rel.) | 2.431419297 |  |  |  |  |  |

Tellurium in BAM-M112:

| 1A | 6.52 | 6.3 | 6.46 | 6.53 |
| :--- | ---: | ---: | ---: | ---: |
| 1E | 6.38 | 6.56 | 6.41 | 6.39 |
| 2A | 6.25 | 6.36 | 6.31 | 6.52 |
| 2E | 6.38 | 6.45 | 6.53 | 6.43 |
| 3A | 6.41 | 6.46 | 6.46 | 6.33 |
| 3E | 6.22 | 6.22 | 6.29 | 6.33 |
| 4A | 6.17 | 6.04 | 6.08 | 6.28 |
| 4E | 6.19 | 6.26 | 6.21 | 6.2 |
| 5A | 6.09 | 6.4 | 6.18 | 6.32 |
| 5E | 6.02 | 6.43 | 6.17 | 6.06 |


| Sample | Number | Sum | Mean | Variance |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sample 1A | 4 | 25.81 | 6.4525 | 0.01129167 |  |  |
| Sample 1B | 4 | 25.74 | 6.435 | 0.0071 |  |  |
| Sample 2A | 4 | 25.44 | 6.36 | 0.0134 |  |  |
| Sample 2B | 4 | 25.79 | 6.4475 | 0.00389167 |  |  |
| Sample 3A | 4 | 25.66 | 6.415 | 0.00376667 |  |  |
| Sample 3B | 4 | 25.06 | 6.265 | 0.00296667 |  |  |
| Sample 4A | 4 | 24.57 | 6.1425 | 0.01135833 |  |  |
| Sample 4B | 4 | 24.86 | 6.215 | 0.00096667 |  |  |
| Sample 5A | 4 | 24.99 | 6.2475 | 0.01929167 |  |  |
| Sample 5B | 4 | 24.68 | 6.17 | 0.03406667 |  |  |
|  |  |  | 6.315 |  |  |  |
|  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares <br> (MS) | F-value | $P$-value | critical F- <br> value |
| Between groups | 0.5229 | 9 | 0.0581 | 5.3746531 | 0.00021471 | 2.21069698 |
| Within groups | 0.3243 | 30 | 0.01081 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 0.8472 | 39 |  |  |  |  |


|  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | :--- |
| within-sd | 0.10397115 |  |  |  |  |  |
|  |  |  |  |  |  |  |
| effective n | 4.00 |  |  |  |  |  |
| s_bb | 0.10873132 |  |  |  |  |  |
| s_bb_min | 0.026415573 |  |  |  |  |  |
| u_bb | 0.10873132 | 108.73132 |  |  |  |  |
|  |  |  |  |  |  |  |
| u_bb(rel.) | 1.721794461 |  |  |  |  |  |

Annex 2: Calculation of uncertainty contribution of potential inhomogeneity (area) Copper in BAM-M112:


| at: Lab. A |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r 0 | 8.53 | 8.67 |  |  |  |  |
| r_in | 8.58 | 8.67 | 8.80 | 8.70 |  |  |
| r_out | 8.55 | 8.73 | 8.78 | 8.64 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | $F$-value | $P$-value | critical F-value |
| Between groups | 0.010875 | 2 | 0.0054375 | 0.584582895 | 0.582399717 | 4.737414128 |
| Within groups | 0.065110526 | 7 | 0.009301504 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 0.075985526 | 9 |  |  |  |  |



| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F-value |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Between groups | 0.27 | 2 | 0.135 | 2.350746269 | 0.165576512 | 4.737414128 |
| Within groups | 0.402 | 7 | 0.057428571 |  |  |  |
| Total | 0.672 | 9 |  |  |  |  |
| within-sd | 0.239642591 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.155695444 |  |  | u_bb (rel.) | 1.6741 |  |
| s_bb_min | 0.097942685 |  |  |  |  |  |
| u_bb | 0.155695444 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  | u_bb (rel.), mean (Labs. $1+5$ ) |  |  | 1.2267 |

Nickel in BAM-M112:

| at: Lab. A |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r 0 | 5.4 |  |  |  |  |  |
| $r$ rin | 5.49 | 5.56 | 5.57 | 5.55 |  |  |
| r_out | 5.46 | 5.47 | 5.54 | 5.53 |  |  |
| at: Lab. B |  |  |  |  |  |  |
| r_0 | 5 |  |  |  |  |  |
| $r$ rin | 5.1 | 5.2 | 5.1 | 5.2 |  |  |
| r out | 5.1 | 5.1 | 5.1 | 5.2 |  |  |
| at: Lab. A |  |  |  |  |  |  |
| $r 0$ | 5.37 | 5.43 |  |  |  |  |
| r_in | 5.49 | 5.56 | 5.57 | 5.55 |  |  |
| r_out | 5.46 | 5.47 | 5.54 | 5.53 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | $F$-value | $P$-value | critical F-value |
| Between groups | 0.027135 | 2 | 0.0135675 | 9.128891231 | 0.011206239 | 4.737414128 |
| Within groups | 0.010403509 | 7 | 0.001486216 |  |  |  |
| Total | 0.037538509 | 9 |  |  |  |  |
| within-sd | 0.038551466 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.061444295 |  |  | u_bb (rel.) | 1.1178 |  |
| s_bb_min | 0.015756106 |  |  |  |  |  |
| u_bb | 0.061444295 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| at: La.b. B |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| r_0 | 4.96 | 5.04 |  |  |  |  |
| r_in | 5.10 | 5.20 | 5.10 | 5.20 |  |  |
| r_out | 5.10 | 5.10 | 5.10 | 5.20 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | $F$-value | $P$-value | critical F-value |
| Between groups | 0.0315 | 2 | 0.01575 | 5.422131148 | 0.037809249 | 4.737414128 |
| Within groups | 0.020333333 | 7 | 0.002904762 |  |  |  |
| Total | 0.051833333 | 9 |  |  |  |  |
| within-sd | 0.053895843 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.063357217 |  |  | u_bb (rel.) | 1.2399 |  |
| s_bb_min | 0.022027402 |  |  |  |  |  |
| u_bb | 0.063357217 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  | u_bb (rel.), mean (Labs. $1+5$ ): |  |  | 1.1804 |

Platinum in BAM-M112:

| at: Lab. A |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r_0 | 5.61 |  |  |  |  |  |
| r_in | 5.88 | 6.07 | 6.06 | 5.8 |  |  |
| r_out | 5.57 | 5.92 | 5.87 | 5.89 |  |  |
| at: Lab. B |  |  |  |  |  |  |
| r_0 | 5.2 |  |  |  |  |  |
| r_in | 5.3 | 5.4 | 5.4 | 5.3 |  |  |
| r_out | 5.3 | 5.4 | 5.6 | 5.5 |  |  |
| at: Lab. A |  |  |  |  |  |  |
| $r$ _0 | 5.50 | 5.72 |  |  |  |  |
| $r$ _in | 5.88 | 6.07 | 6.06 | 5.80 |  |  |
| r_out | 5.57 | 5.92 | 5.87 | 5.89 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F-value |
| Between groups | 0.15801 | 2 | 0.079005 | 3.523864592 | 0.087341712 | 4.737414128 |
| Within groups | 0.156939912 | 7 | 0.022419987 |  |  |  |
| Total | 0.314949912 | 9 |  |  |  |  |
| within-sd | 0.149733054 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.132976751 |  |  | u_bb (rel.) | 2.2817 |  |
| s_bb_min | 0.061196373 |  |  |  |  |  |
| u_bb | 0.132976751 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| at: Lab. B |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| r_0 | 5.12 | 5.28 |  |  |  |  |
| r_in | 5.30 | 5.40 | 5.40 | 5.30 |  |  |
| r_out | 5.30 | 5.40 | 5.60 | 5.50 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F-value |
| Between groups | 0.084 | 2 | 0.042 | 4.121495327 | 0.065629259 | 4.737414128 |
| Within groups | 0.071333333 | 7 | 0.010190476 |  |  |  |
| Total | 0.155333333 | 9 |  |  |  |  |
| within-sd | 0.100947888 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.099701937 |  |  | u_bb (rel.) | 1.8601 |  |
| s_bb_min | 0.041257721 |  |  |  |  |  |
| u_bb | 0.099701937 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  | u_bb (rel.), mean (Labs. $1+5$ ) |  |  | 2.0816 |

Selenium in BAM-M112:

| at: |  | Lab. A |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $r$ r 0 | 4.52 |  |  |  |  |  |
| r_in | 4.6 | 4.58 | 4.66 | 4.49 |  |  |
| r_out | 4.65 | 4.48 | 4.46 | 4.5 |  |  |
| at: |  | Lab. B |  |  |  |  |
| r_0 | 4.2 |  |  |  |  |  |
| r_in | 4.16 | 4.41 | 4.66 | 4.72 |  |  |
| r_out | 4.41 | 4.28 | 4.53 | 4.66 |  |  |
| at: |  | Lab. A |  |  |  |  |
| r_0 | 4.46 | 4.58 |  |  |  |  |
| r_in | 4.60 | 4.58 | 4.66 | 4.49 |  |  |
| r_out | 4.65 | 4.48 | 4.46 | 4.50 |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F-value |
| Between groups | 0.00889 | 2 | 0.004445 | 0.708635415 | 0.524497698 | 4.737414128 |
| Within groups | 0.043908333 | 7 | 0.006272619 |  |  |  |
| Total | 0.052798333 | 9 |  |  |  |  |
| within-sd | 0.079199868 |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0 |  |  | u_bb (rel.) | 0.7120 |  |
| s_bb_min | 0.032369237 |  |  |  |  |  |
| u_bb | 0.032369237 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| at: |  | Lab. B |  |  |  |  |
|  |  |  |  |  |  |  |
| r_0 | 4.05 | 4.35 |  |  |  |  |
| r_in | 4.16 | 4.41 | 4.66 | 4.72 |  |  |
| r_out | 4.41 | 4.28 | 4.53 | 4.66 |  |  |
|  |  |  |  |  |  |  |
| Source of variation | sums of squares (SS) | degrees of freedom (df) | Mean squares (MS) | F-value | $P$-value | critical F-value |
| Between groups | 0.124364198 | 2 | 0.062182099 | 1.346935159 | 0.319965329 | 4.737414128 |
| Within groups | 0.323159351 | 7 | 0.046165622 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 0.447523548 | 9 |  |  |  |  |
|  |  |  |  |  |  |  |
| within-sd | 0.214861866 |  |  |  |  |  |
|  |  |  |  |  |  |  |
| effective n | 3.20 |  |  |  |  |  |
| s_bb | 0.070747079 |  |  | u_bb (rel.) | 1.9856 |  |
| s_bb_min | 0.087814725 |  |  |  |  |  |
| u_bb | 0.087814725 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  | u_bb (rel.), mean (Labs. $1+5$ ): |  |  | 1.4916 |

Tellurium in BAM-M112:


